

Integer and Nonlinear Optimization

Exercise 14

Problem 1 (6 points)

Prove that the search directions $\bar{d}^1, \dots, \bar{d}^n \in \mathbb{R}^n$ computed in each iteration of the method of Rosenbrock (Algorithm 12.5) are linearly independent and orthogonal for any set of $\lambda_1, \dots, \lambda_n$ computed in Step 2a.

Furthermore, show that if $\lambda_j = 0$ then $\bar{d}^j = d^j$.

Problem 2 (18 points)

Implement each of the following algorithms in Matlab and submit the *running* programs to pfeiffer@am.uni-erlangen.de.

- (a) Cyclic coordinate method
- (b) Method of Hooke and Jeeves
- (c) Steepest descent method
- (d) Conjugate gradient method of Fletcher and Reeves.

Find the minimum of $f(x_1, x_2) = (x_1^3 - x_2)^2 + 2(x_2 - x_1)^4$ by each of the four procedures, starting with $\underline{x}_1 = (1, 0)^T$ and $\varepsilon = \frac{1}{4}$. Illustrate the procedures in a graph showing the level curves of the function.