Standort-Optimierung Handout 6



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Algorithm 6.7: Branch and Bound Algorithm for $\#/D/\bullet/\bullet/\sum_{cov}$

- Input: Finite set of demand nodes I, finite set of candidate sites J, $a_{ij} \in \{0, 1\} \ \forall i \in I, j \in J.$
- Step 1: Initial solution: Apply the reduction rules 1, 2a and 2b to obtain a reduced IP-formulation of the problem. Let \bar{z} be an upper bound on the optimal objective value (suffi-
- Step 2: Initial relaxation: Solve the LP-relaxation of the problem determined in Step 1 and let \underline{z}_1 be its objective value (lower bound). Node P_1 of the Branch and Bound tree represents the present problem and is the only live node.
- Step 3: Branch and Bound procedure: Does any live node exist in the solution tree? If yes: Choose a live node P. (a.g. the po

ciently large).

- If yes: Choose a live node P_k (e.g., the node with the best lower bound \underline{z}_k), and go o Step 4.
- If no: The best known feasible solution is optimal. (If no such solution is known, the problem is infeasible.)

Step 4: Is the solution represented by node P_k feasible (for the original problem)?

If yes: (STOP), the solution in node P_k is optimal. If no: Goto Step 5.

Step 5: Branching:

Select a decision variable x whose value in the relaxed problem at node P_k is $x = \gamma \notin \mathbb{N}$ but must be integer in a feasible solution. Branch from node P_k to nodes P_{s+1} , P_{s+2} , so that, in addition to the constraints added earlier, at node P_{s+1} we set $x \leq \lfloor \gamma \rfloor$ and at node P_{s+2} we set $x \geq \lceil \gamma \rceil$.

Step 6: Bounding:

For each node P_{s+k} , k = 1, 2, do: Solve the LP relaxation including the constraints added in Step 5. Let its objective value be \underline{z}_{s+k} . If $\underline{z}_{s+k} \geq \overline{z}$, fathom node P_{s+k} . If $\underline{z}_{s+k} < \overline{z}$ and the solution is feasible, set $\overline{z} := \underline{z}_{s+k}$ and fathom node P_{s+k} . If $\underline{z}_{s+k} < \overline{z}$ and the solution is infeasible, the node P_{s+k} is live. Goto Step 3.

Output: Optimal solution of $\#/D/ \bullet / \bullet / \sum_{cov}$ with objective value \bar{z} .