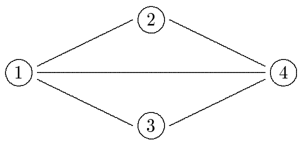
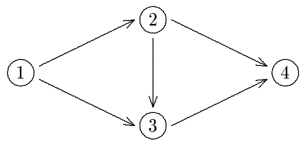
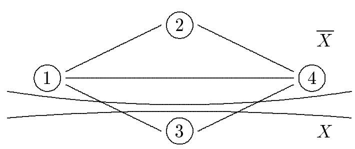
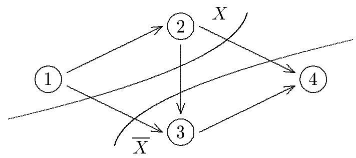
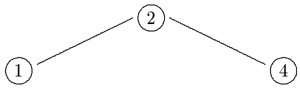
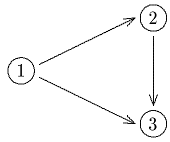
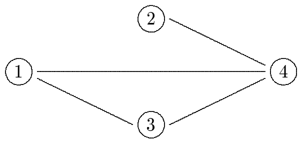
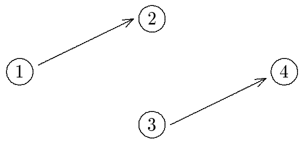
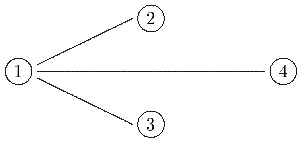
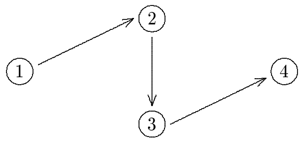
	graph G	digraph G
		
nodes	$N = \{1, 2, 3, 4\}$	$N = \{1, 2, 3, 4\}$
arcs	$A = \{[1,2], [1,3], [1,4],$ $[2,4], [3,4]\}$	$A = \{(1,2), (1,3), (2,3),$ $(2,4), (3,4)\}$
degree indegree outdegree	$d(1) = 3$	$d(3) = 3$ $d^-(3) = 2$ $d^+(3) = 1$
path: not simple	$P = (1, 2, 4, 1, 3),\ l = 4$	$P = (1, 2, 4, 3, 2, 4),\ l = 5$ $P^+ = \{(1,2), (2,4)\}$ $P^- = \{(3,4), (2,3)\}$
simple	$P = (1, 2, 4, 3),\ l = 3$	$P = (1, 2, 4, 3),\ l = 3$ $P^+ = \{(1,2), (2,4)\}$ $P^- = \{(3,4)\}$
dipath		$P = (1, 2, 3, 4)$
cycle	$C = (1, 2, 4, 1)$	$C = (1, 2, 3, 1)$
dicycle		does not exist
G acyclic?	no	yes
connectedness	is connected	is connected
disconnecting set of arcs	$Q = \{[1,3], [3,4], [1,4]\}$	$Q = \{(1,2), (1,3), (3,4)\}$
cut	$Q = \{[1,3], [3,4]\} = (X, \overline{X})$ with $X = \{3\},\ \overline{X} = \{1, 2, 4\}$ 	$Q = \{(1,3), (2,3), (2,4)\} = (X, \overline{X})$ with $X = \{1, 2\},\ \overline{X} = \{3, 4\}$; $Q^+ = Q,\ Q^- = \emptyset$ 

subgraph		
spanning subgraph		
spanning tree T of G		
leaf nodes of T	$\{2, 3, 4\}$	$\{1, 4\}$
incidence matrix	$\mathcal{N} = \begin{pmatrix} 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{pmatrix}$	$\mathcal{N} = \begin{pmatrix} 1 & 1 & 0 & 0 & 0 \\ -1 & 0 & 1 & 1 & 0 \\ 0 & -1 & -1 & 0 & 1 \\ 0 & 0 & 0 & -1 & -1 \end{pmatrix}$
adjacency matrix	$\mathcal{H} = \begin{pmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$	$\mathcal{H} = \begin{pmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$

Trees and spanning trees have the following properties:

Lemma: Let $T = (N, A(T))$ be a spanning tree of $G = (N, A)$. Then:

(a) If $|N| \geq 2$, then T has at least two leaf nodes.

(b) T has exactly $n - 1$ arcs.

(c) Every pair of nodes in T is connected by exactly one path.

(d) $T + a := (N, A(T) \cup \{a\})$ contains exactly one cycle $(\forall\, a \in A \setminus A(T))$.

(e) If $a \in A \setminus A(T)$ and if C is the uniquely defined cycle in $T + a$, then $T + a \setminus \tilde{a} := (N, A(T) \cup \{a\} \setminus \{\tilde{a}\})$, $\forall\, \tilde{a} \in C$, is a spanning tree.

(f) $T \setminus a := (N, A(T) \setminus \{a\})$ consists of two subtrees $(X, A(X))$ and $(\overline{X}, A(\overline{X}))$. Furthermore, $Q = (X, \overline{X})$ is a cut in G $(\forall\, a \in A(T))$.

(g) If $a \in A(T)$ and if $Q = (X, \overline{X})$ is the uniquely defined cut in G (cf. (f)), then $T \setminus a + \tilde{a} := (N, A(T) \setminus \{a\} \cup \{\tilde{a}\})$, $\forall\, \tilde{a} \in (X, \overline{X})$, is a spanning tree.